

2009-2010 7TH GRADE CONTEST SOLUTIONS

Answers

30. If A , B , and C are on a line, the distance from point A to point C can be 3 cm or 11 cm. Otherwise, the distance from point A to point C is between 3 cm and 11 cm.

A) 2 cm B) 3 cm C) 6 cm D) 10 cm

30.

A

31. Since $S \times RS$ has 3 digits and a ones digit of S , S is 5 or 6. If S is 5, RS must be 2 or 3, since the product begins with 1. Only 3 works, since $T > S$. If $S = 6$ and $R = 2$, $T = 5 < S$, which is not allowed.

A) 1 B) 4 C) 5 D) 6

31.

C

32. Can the sides be 10, 10, and 20? No: the sum of the two smaller sides must be greater than the 3rd side. So the sides are 10, 20, and 20; the perimeter is 50.

A) 60 B) 50 C) 40 D) 30

32.

B

$$33. \frac{9}{2} - \frac{2}{9} = \frac{81}{18} - \frac{4}{18} = \frac{77}{18}.$$

A) $\frac{18}{77}$ B) $\frac{14}{18}$ C) $\frac{18}{14}$ D) $\frac{77}{18}$

33.

D

34. The numbers are the even sums $2+2$, $2+4$, $2+2$, $2+4$, $2+6$, ..., $2+196$. There are 98 such sums from 4 to 198.

A) 101 B) 100 C) 99 D) 98



34.

D

35. In 1 hour, the wheel rolls $30 \times 200\pi$ m = 6000π m. Its circumference is $(2 \times \pi \times 2)$ m = 4π m. It makes 6000π m \div 4π m = 1500 full revolutions.

A) 100 B) 200 C) 1500 D) 3000

35.

C

36. The product must be divisible by 210 because $2 \times 3 \times 5 \times 7 = 210$.

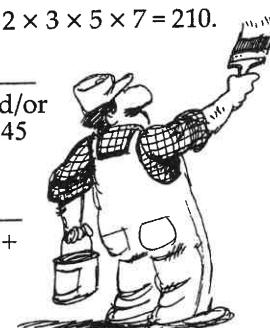
A) 210 B) 260 C) 420 D) 520

36.

A

37. Of 180 paintings, $180 - 25 = 155$ have blue and/or red borders. Since $110 + 90 = 200$, $200 - 155 = 45$ have borders with both colors.

A) 25 B) 45 C) 55 D) 65



37.

B

$$38. \text{The difference is } (2+4+6+\dots+100) - (1+3+5+\dots+99) = (2-1) + (4-3) + (6-5) + \dots + (100-99) = 1 + 1 + 1 + \dots + 1 = 50.$$

A) 100 B) 50 C) 25 D) 1

38.

B

39. Ones digits of powers of 2 cycle 2, 4, 8, 6, 2, 4, 8, 6 ... ; $2009 \div 4$ has R1.

A) 2^{2009} B) 2^{2010} C) 2^{2011} D) 2^{2012}

39.

A

40. Work backwards: Gwen had $\frac{3}{2} \times \$36 = \54 before buying clothes.

Gwen had $\frac{7}{6} \times \$54 = \63 before buying food, so she spent \$9 on food.

A) \$24 B) \$18 C) \$12 D) \$9

40.

D

The end of the contest



Information & Solutions

2009-2010 Annual 7th Grade Contest

Tuesday, February 16 or 23, 2010

7

Contest Information

- **Solutions** Turn the page for detailed contest solutions (written in the question boxes) and letter answers (written in the *Answer Column* to the right of each question).
- **Scores** Please remember that *this is a contest, and not a test*—there is no “passing” or “failing” score. Few students score as high as 30 points (75% correct); students with half that, 15 points, deserve commendation!
- **Answers and Rating Scales** Turn to page 141 for the letter answers to each question and the rating scale for this contest.



16.	A) 12 B) 24 C) 36 D) 48	17.	A) 12 m B) 10 m C) 8 m D) 5 m
18.	A) 0.9 B) 9 C) 90 D) 900	19.	A) $\frac{100}{300}$ B) $\frac{150}{300}$ C) $\frac{990}{3000}$ D) $\frac{1001}{3000}$
20.	A) 0.1 B) 0.5 C) 10 D) 20	21.	A) 60 B) 90 C) 120 D) 180
21.		22.	Since $300 \div 26$ has a quotient of 11 and a remainder of 14, the 300th letter written is the 14th one from the beginning of the alphabet, N.
22.	A) K B) L C) M D) N	23.	23. The sum of Linda's first 4 grades is $4 \times 75 = 300$. The sum of her first 5 is $5 \times 80 = 400$. Her score on the 5th test is the difference: $400 - 300 = 100$.
23.	A) 100 B) 95 C) 85 D) 80	24.	A) 10 m + 10 cm = 10 m + 0.1 m = 10.1 m.
24.		25.	25. $18:12 = 3:2 = (3 \times 12):(2 \times 12) = 36:24$.
25.		26.	A) 10:00 AM B) 11:52 AM C) 11:56 AM D) 12:02 PM
26.		27.	27. $(4+52)$ minutes after 10:56 AM is 11:52 AM.
27.	D	28.	The square of the reciprocal is $\frac{1}{9}$, so the square of the number is 9, the number is 3, and the number's cube is $3^3 = 3 \times 3 \times 3 = 27$.
28.	A) $\frac{1}{27}$ B) $\frac{1}{9}$ C) 9 D) 27	29.	29. It goes 240 000 m in 60 mins, 4000 m in 1 min, 2000 m in 30 seconds.
29.	A) 2 B) 8 C) 2000 D) 8000		C

1.		Answers
2.	Work backwards: $4 \times 18 + 2 = 72 + 2 = 74$.	B
3.	A) 2.34 B) 2.35 C) 2.35 D) 2.5	C
4.	A) $\{b\}$ B) $\{b, c\}$ C) $\{a, d\}$ D) $\{a, b, c, d\}$	D
5.	From 1 to 99 is 99 numbers. Subtract the first 20 numbers to get 79.	E = MC ²
6.	A) 81 B) 80 C) 79 D) 78	
7.	As shown below, only choice B is a prime number.	B
8.	A) $81 = 9 \times 9$ B) 83 C) $87 = 3 \times 29$ D) $99 = 9 \times 11$	C
9.	A) $\sqrt[3]{6} - \sqrt[3]{5} = 6 - 5 = 1 = \sqrt[3]{1}$.	A
10.	10. There are 40 quarters in a roll. Each sister's share is $40 \div 8 = 5$, so three sisters take 15 coins, leaving 25 quarters in the roll. The value of these 25 quarters is $25 \times 25 = \$6.25$.	
11.	A) 2^5 B) 4^8 C) 3^4 D) 2^8	A
12.	12. A hexagon has 6 sides and an octagon has 8 sides. The ratio is $6:8 = 3:4$.	
13.	13. The average is $\left(\frac{1}{2} + \frac{1}{3}\right) \div 2 = \frac{5}{6} \times \frac{1}{2} = \frac{5}{12}$.	D
14.	14. $(3 \times 2 \times 6 \times 2 \times 9 \times 2 \times 12 \times 2) \div (3 \times 6 \times 9 \times 12) = 2 \times 2 \times 2 = 16$.	A
15.	15. A circle's radius, r , divided by its circumference, $2\pi r$, has quotient $1/(2\pi)$.	D